

Mechanical Behavior and Microstructure of SiC and SiC/TiB₂ Ceramics

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Abstract

Toughness characteristics and associated microstructural behavior in two kinds of SiC and TiB₂ particulate-reinforced SiC composites were studied. From indentation-strength tests, the Al₂O₃-doped, high volume fraction β -SiC/TiB₂ showed a distinctive flaw tolerance and a higher retained strength in the long-crack region, as compared with β -SiC alone. On the other hand, the boron- and carbon-doped, low volume fraction, α -SiC/TiB₂ exhibited a higher retained strength without an apparent improvement in flaw tolerance, as compared with α -SiC. Crack bridging and sliding and pullout of TiB₂ particulates toughened the β -SiC/TiB₂, while only crack bridging by TiB₂ occurred in α -SiC/TiB₂ with difficulty in grain sliding and pullout. A quantitative evaluation of the indentation-strength data revealed a sharp rising toughness curve for β -SiC/TiB₂. The enhanced long-crack toughness originated from the weak interface created by the TiB₂ and sintering additives. © 1997 Elsevier Science Limited.

1 Introduction

Silicon carbide (SiC) is one of the important structural ceramics for high temperature applications because of its excellent mechanical properties. However, its low fracture toughness and the high flaw sensitivity limit its widespread applications.

It has been demonstrated that the fracture toughness and the flaw tolerance of ceramics can be improved by controlling the microstructure and by incorporating second phases (particulates, whiskers). By in-situ forming of elongated-shaped reinforcements, significant improvements in flaw tolerance and toughening have been achieved in silicon nitride.^{1,2} Different sintering additives have been

used to densify SiC and to modify its microstructure. The liquid-phase-sintered SiC densified with Al₂O₃ and Y₂O₃ as sintering additives exhibits a fracture toughness as high as 7 MPa·m^{1/2}.^{3–5} SiC also has been reinforced by TiC^{6,7} and TiB₂^{8–12} particles as a dispersed phase to improve fracture toughness. The SiC/TiB₂ composite has shown a low electrical resistivity (< 1 Ω ·cm), which makes it a good electrical conductor and has good electrical-discharge machinability.⁸ The flexural strength, fracture toughness, and toughness-curve (R- or T-curve) of pressureless sintered SiC composites reinforced with TiB₂ have been measured.^{8–12} Toughening mechanisms such as crack deflection, crack bridging, and microcracking have been proposed for this material. As a major candidate for armor ceramics, the retained strength (post-damage strength) of the SiC/TiB₂ composite is an important indicator of the performance of armors.¹³ However, the retained strength behavior of SiC/TiB₂ has not yet been discussed.

In the present study, indentation-strength tests were used to determine the retained strength (post-indentation strength), flaw tolerance, and toughness-curve characteristics of two kinds of SiC and SiC/TiB₂ composites. β -SiC and, β -SiC/TiB₂ composites which were hot pressed with an Al₂O₃ sintering aid, were compared with the well-studied α -SiC and α -SiC/TiB₂ composites, which were sintered with boron and carbon additives. The effects of microstructural changes resulting from the sintering additives, as well as from TiB₂ content on the toughening behavior and flaw tolerance for these materials have been investigated.

2 Experimental Procedure

Four materials of SiC and its composites reinforced with TiB₂ were investigated. A commercial α -SiC (Hexoloy SA) and a 15 vol% TiB₂/ α -SiC composite (α -SiC/TiB₂, Hexoloy ST) were obtained from the Carborundum company, Niagara Falls, NY.

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They were sintered at temperatures above 2000°C using boron and carbon as sintering aids in an inert atmosphere.⁸ They had 3–8- μm grain sizes for SiC and 1–5- μm particle sizes for the discrete TiB₂ particles. A β -SiC and a 30-vol% TiB₂/ β -SiC composite (β -SiC/TiB₂) were supplied by the Alcoa company, Alcoa Center, PA. They were hot-pressed at 1950°C under 18 MPa in an argon atmosphere for 2 h, using Al₂O₃ as a sintering aid. β -SiC single phase material had a grain size ranging from 0.8 to 3 μm . The TiB₂ particles, with particle sizes ranging from 3 to 8 μm in the β -SiC matrix, were not fully discrete, but tended to be adjacent to other TiB₂ particles.

Mechanical testing was carried out on rectangular beams using the indentation-strength method. Because of the confirmation of stable crack growth of SiC/TiB₂ by Gu and Faber¹⁰ using the double cantilever beam technique and the confirmation of indentation parameters of χ on SiC by Padture and Lawn,¹⁴ this test technique can be applied to measure T curve with confidence. Specimens had dimensions of 25 \times 2.5 (width) \times 2.2 (depth) mm. Specimen surfaces were polished down to a 1- μm diamond paste finish and the edges of the tensile surfaces were bevelled with a 3- μm diamond paste. Specimens for flexural tests were indented in air at the center of tensile surfaces, with a Vickers diamond pyramid, at constant loads from $P=2$ to 300 N. Some flexural bars were left without Vickers indentations, for measurement of 4-pt flexural strengths.

The rectangular bars were tested in a four-point bend fixture (20 mm outer span and 10 mm inner span) mounted on a universal testing machine (Model 4502, Instron, Canton, MA). To lessen environmental effects, a drop of silicone oil was placed on the indented site, and the bar was broken in rapid loading (failure time < 10 ms). If the flexural failures of the bars did not originate from the indentations, these calculated strengths were included in the 4-pt flexural strengths. Average strength values with one standard deviation from four or five successful tests, were measured as a function of indentation load.

To construct the toughness curve, the Vickers hardness was obtained by the indentation technique. Young's modulus was obtained by the pulse echo, ultrasonic technique (NDT-150, Nortec Inc., Kennewick, WA). Fracture behavior was analyzed by scanning electron microscopy (SEM, Model DS-130, International Scientific Instruments, Santa Clara, CA). Transmission electron microscopy (TEM, Model CM-12, Philips Instruments, Inc., Mahwah, NJ) and energy dispersive spectroscopy (EDS, Model EDAX-9900, EDAX International, Prairie View, IL) were used to characterize

the microstructure and microchemistry, respectively.

3 Results

3.1 Observation of crack–microstructure interactions

SEM crack propagation profiles of radial cracks by Vickers indentation tests on SiC are shown in Fig. 1. In the boron- and carbon-doped α -SiC,

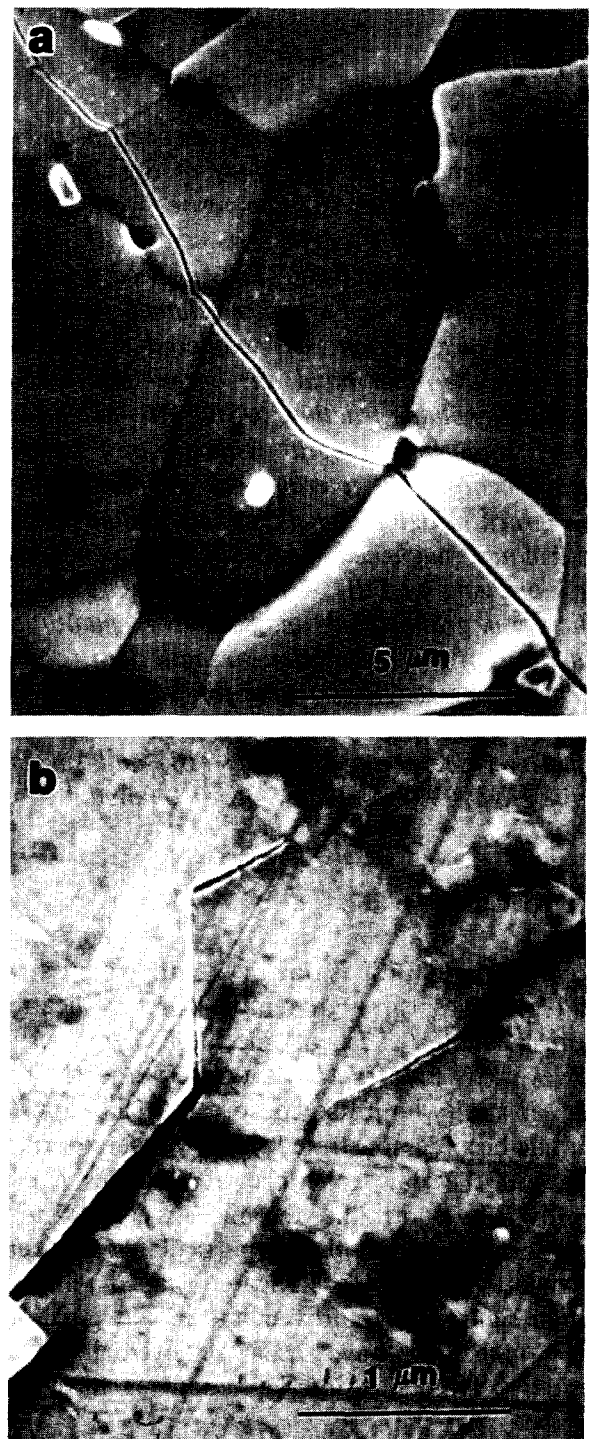


Fig. 1. (a) Transgranularly fractured boron- and carbon-doped α -SiC and (b) intergranularly fractured Al₂O₃-doped β -SiC showing crack bridging after Vickers indentation.

transgranular fracture occurred, as seen in Fig. 1(a). However, intergranular fracture was observed in Al doped β -SiC. Crack bridging by grains located at the radial crack tips was observed in SiC, as seen in Fig. 1(b).

In the composites, cracks usually deflected around or were bridged by TiB₂ particles. A typical crack bridging by a TiB₂ particle in α - and β -SiC/TiB₂ near a radial crack tip was evidenced in Fig. 2(a) and (b), respectively. Although the

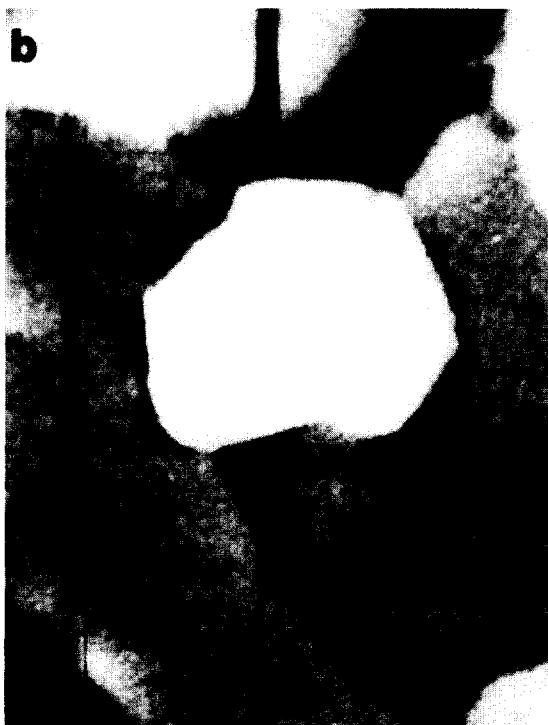
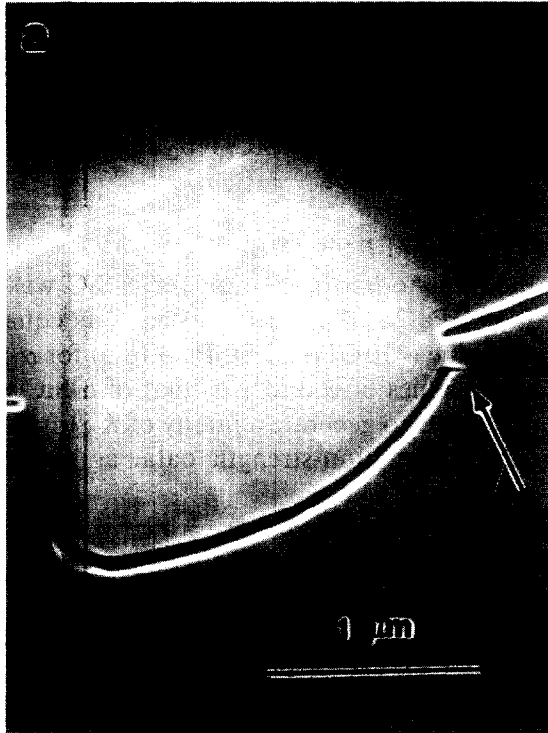


Fig. 2. Bridging behavior of a TiB₂ particle in (a) α -SiC/TiB₂ and β -SiC/TiB₂. The arrow in (a) indicates the evidence of crack bridging behavior.

bridged TiB₂ posed a crack closure force to toughen these composites, the TiB₂ in the α -SiC/TiB₂ had much difficulty in sliding and pullout. Instead a crack [arrowed in Fig. 2(a)] initiated at the debond crack as the applied load increased.

3.2 Indentation-strength and toughness curves

Results of the indentation load (P)-strength (σ_F) testing are presented in Fig. 3 for α -SiC and α -SiC/TiB₂, and in Fig. 4 for β -SiC and β -SiC/TiB₂. As shown in Figs 3 and 4, the fracture strengths of unindented α -SiC, α -SiC/TiB₂, β -SiC, and β -SiC/TiB₂ were 458 ± 35 , 465 ± 39 , 394 ± 32 , and 327 ± 40 MPa, respectively. The fracture strengths of α -SiC and α -SiC/TiB₂ were close to each other. The slope for α -SiC was close to $-1/3$, which indicated a single-valued toughness. The $\sigma_F(P)$ response of α -SiC/TiB₂ deviated slightly from the $P^{-1/3}$ dependence, which was expected to have a

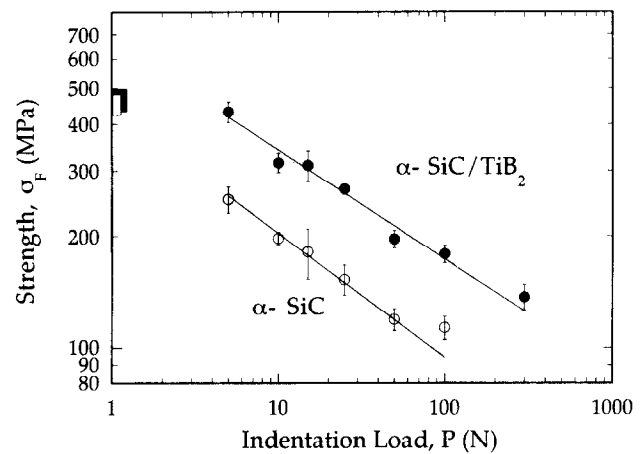


Fig. 3. Indentation-strength data for α -SiC and α -SiC/TiB₂. Boxes on the left axis are strengths representing data from unindented specimens. The line passing through α -SiC data is the line of best fit for the condition $\sigma_F \propto P^{-1/3}$. The line for α -SiC/TiB₂ is the linear least-squares fit to the data.

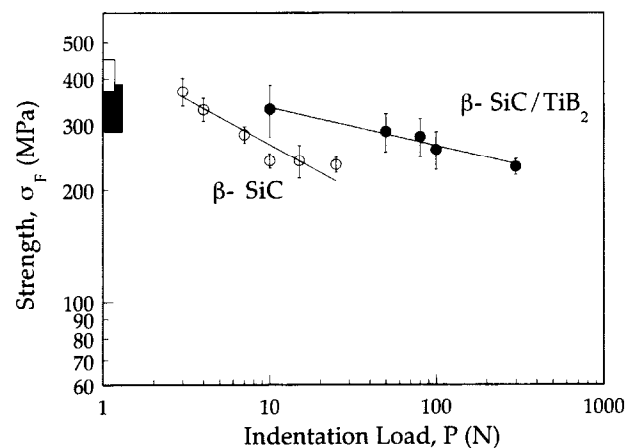


Fig. 4. Indentation-strength data for β -SiC and β -SiC/TiB₂. Boxes on the left axis are strengths representing data from unindented specimens. The lines are the linear least-squares fit to the data.

slightly rising toughness curve $T(c)$. The main effect of TiB_2 in the $\alpha\text{-SiC}/\text{TiB}_2$ was to increase the retained strength (post-indentation strength) of SiC, rather than on flaw tolerance (relative to the slope of the $\sigma_F(P)$ response). On the other hand, the fracture strength of $\beta\text{-SiC}$ decreased as 30 vol% TiB_2 was added. Both $\beta\text{-SiC}$ and SiC/TiB_2 , exhibited flaw tolerance, especially $\beta\text{-SiC}/\text{TiB}_2$, which showed a strongly enhanced long-crack strength (Fig. 4). The significant flaw tolerance of $\beta\text{-SiC}/\text{TiB}_2$ corresponds to the near-flat slope of the $\sigma_F(P)$ response. The effect of TiB_2 in $\beta\text{-SiC}/\text{TiB}_2$ was to increase the retained strength at the long-crack region and to enhance the flaw tolerance.

Toughness curves $T(c)$ can be deconvoluted from the data in Figs 3 and 4 in accordance with an indentation-strength K-field analysis suggested by Mai and Lawn¹⁵ and Lawn.¹⁶ Under the action of an applied stress σ_A , radial cracks of size c produced at an indentation load P extend according to the equilibrium condition⁽¹⁵⁾

$$K_A'(c) = \psi\sigma_A c^{1/2} + \chi P/c^{3/2} = T(c) \quad (1)$$

where $K_A'(c)$ is an effective applied stress intensity factor and $T(c)$ defines the toughness curve for the material; ψ is a geometrical coefficient that characterizes the crack configuration;¹⁷ and $\chi\alpha(E/H)^{1/2}$ is a residual-contact coefficient.^{17,18} For a given load P , failure occurs at that applied stress $\sigma_A = \sigma_F$, which corresponds to a 'tangency condition'

$$dK_A'(c)/dc = dT(c)/dc \quad (2)$$

Accordingly, if the coefficients ψ and χ can be properly calibrated, families of curves can be generated from the data in Figs 3 and 4. Toughness curves $T(c)$ should be determined as envelopes to these families of curves.¹⁹ Such constructions for SiC and SiC/TiB_2 are made below.

3.2.1. $\alpha\text{-SiC}$ and $\alpha\text{-SiC}/\text{TiB}_2$

The construction of a toughness curve for $\alpha\text{-SiC}$ has been demonstrated by Pature and Lawn,¹⁴ by assuming that material-independent $\psi = 0.77$ and $\chi = 0.067$, after calibration with the well studied Al_2O_3 . In this study, these parameters were followed, except for the χ value of $\alpha\text{-SiC}/\text{TiB}_2$. According to the relationship of $\chi\alpha(E/H)^{1/2}$, the modulus-to-hardness ratio for $\alpha\text{-SiC}/\text{TiB}_2$ was $(E/H) = (420 \text{ GPa}/29.7 \text{ GPa}) = 14.1$ and χ was calibrated to be 0.062. As the $\sigma_F(P)$ response followed the $P^{-1/3}$ dependence, $\alpha\text{-SiC}$ had a toughness, $T(c) = T_0 = \text{constant}$. By solving eqns (1) and (2) with $T = T_0$ at the condition of crack growth instability ($d\sigma_A/dc = 0$), we can obtain¹⁹

$$\sigma_A = \sigma_F = (3T_0/4\psi)(T_0/4\chi P)^{1/3} \quad (3)$$

From the data in Fig. 3, the T_0 value can be obtained for the known brittle $\alpha\text{-SiC}$ by curve-fitting the data to eqn (3). The best-fit line in Fig. 3 for $\alpha\text{-SiC}$ corresponds to the condition under $T_0 = 2.2 \text{ MPa}\cdot\text{m}^{1/2}$. Families of $K_A'(c)$ curves can be generated from the indentation-strength data in Fig. 3 and eqn (1) for $\alpha\text{-SiC}$ [Fig. 5(a)] and $\alpha\text{-SiC}/\text{TiB}_2$ [Fig. 5(b)], respectively. It was apparent that the envelope of tangency points was approximately horizontal for $\alpha\text{-SiC}$, while it slightly increased for $\alpha\text{-SiC}/\text{TiB}_2$. The horizontal envelope indicated a single-valued toughness for $\alpha\text{-SiC}$. The slightly increased envelope for $\alpha\text{-SiC}/\text{TiB}_2$ suggested a limited toughening effect.

3.2.2. $\beta\text{-SiC}$ and $\beta\text{-SiC}/\text{TiB}_2$

The modulus-to-hardness ratio for $\beta\text{-SiC}$ was $(E/H) = (430 \text{ GPa}/26 \text{ GPa}) = 16.5$, which was equal to an E/H value $(410 \text{ GPa}/24.5 \text{ GPa}) = 16.5$ for $\alpha\text{-SiC}$. The same values of ψ and χ as that of $\alpha\text{-SiC}$ were used for $\beta\text{-SiC}$ to generate a family of $K_A'(c)$ curves from the indentation-strength data, as shown in

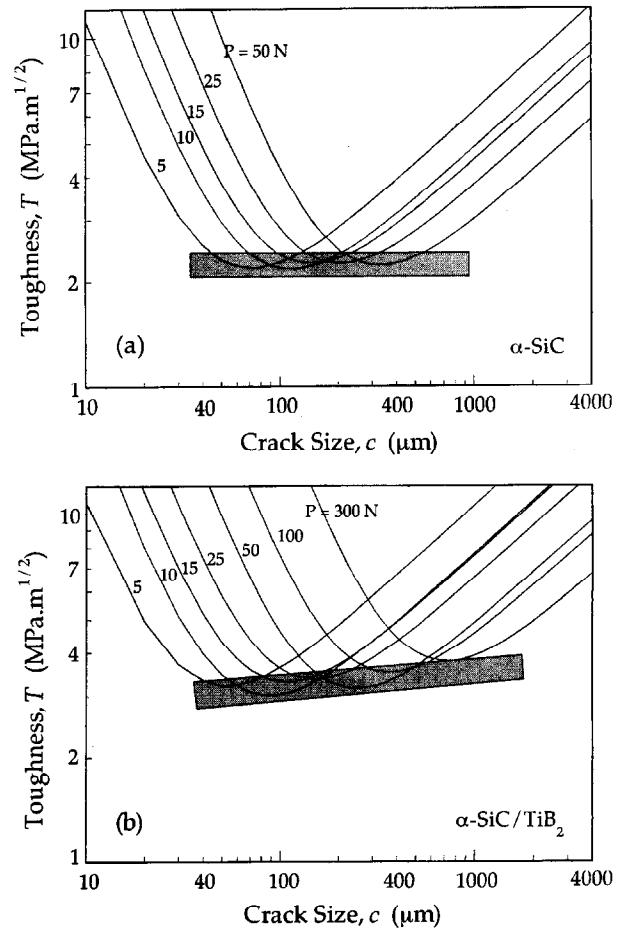


Fig. 5. Toughness-curve diagrams for (a) $\alpha\text{-SiC}$ and (b) $\alpha\text{-SiC}/\text{TiB}_2$. The family of solid curves are plots of $K_A'(c)$ in eqn (1), using strength data from Fig. 3. Shaded bands are T -curves, plotted as locus of tangency points to $K_A'(c)$ curves.

Fig. 6(a). The modulus-to-hardness ratio for β -SiC/TiB₂ was $(E/H) = (430 \text{ GPa}/33.6 \text{ GPa}) = 12.8$. The χ value was modified to be 0.059 for β -SiC/TiB₂. A family of $K_A'(c)$ curves generated from the indentation-strength data in Fig. 4 is shown in Fig. 6(b) for β -SiC/TiB₂. We observed that the envelope of tangency points only slightly increased for α -SiC, while yielding a rising $T(c)$ curve for β -SiC/TiB₂. In the long crack region, the toughness of β -SiC/TiB₂ increased relative to the β -SiC by a factor of ~ 3 .

4 Discussion

Boron and carbon for sintering the α -type materials formed granules at grain boundaries (Fig. 7). The transgranular fracture occurring in α -SiC [Fig. 1(a)] indicated strong bonding between SiC grains. A slightly rising $T(c)$ curve for α -SiC/TiB₂ arose mainly from the TiB₂ contribution. As seen in Fig. 2(a), the crack was bridged by a TiB₂ particle. The T -curve behavior was due mainly to crack bridging in non-transformable, non-cubic

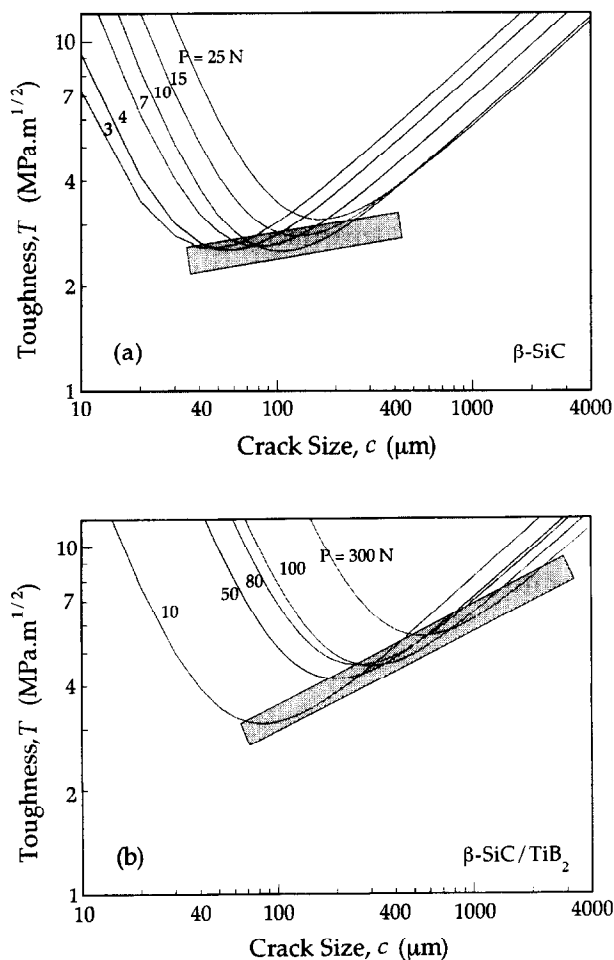


Fig. 6. Toughness-curve diagrams for (a) β -SiC and (b) β -SiC/TiB₂. The family of solid curves are plots of $K_A'(c)$ in eqn (1), using strength data from Fig. 4. Shaded bands are T -curves plotted as locus of tangency points to $K_A'(c)$ curves.



Fig. 7. TEM micrograph of a sintering aid granule at grain boundaries commonly found in α -SiC and α -SiC/TiB₂.

materials.²⁰ For crack bridging, the interface debonding between SiC and TiB₂ first needed to occur. The sources of a debonding interface were: (1) no chemical reactions between SiC and TiB₂ and (2) residual stresses at the interface. There was a thermal expansion mismatch between SiC ($\alpha = 5.6 \times 10^{-6} \text{ K}^{-1}$) and TiB₂ ($\alpha = 8.5 \times 10^{-6} \text{ K}^{-1}$), which caused residual stresses.¹⁰ The residual tensile stress in the TiB₂ particulates enhanced debonding at the interface. Although the interface debonding occurred, it was not weak enough to enable TiB₂ sliding and pullout easily which limited the toughening effect. This behavior was demonstrated by an arrow indicated in Fig. 2(a). The slightly strong interface between SiC and TiB₂ explained the increases in the strength and retained strength as TiB₂ was added to the matrix (Fig. 3). On the other hand, another toughening mechanism of stress-induced microcracking in α -SiC/TiB₂ has been proposed by Gu and Faber.^{10,11}

Crack bridging also has been observed in Fig. 1(b) and 2(b) for β -SiC and its composite. Although crack deflection was observed, the rising $T(c)$ curve for β -SiC/TiB₂ could not be explained by a crack deflection model.²⁰ The residual stress effect between SiC and TiB₂, similar to α -type SiC materials, was a possible reason. The other contribution to interfacial debonding and a sharp T curve came from the intergranular phases in β -SiC and β -SiC/TiB₂. Amorphous silica between grains [Fig. 8(a)] and a crystalline aluminum silicate at a triple point [Fig. 8(b)] were observed and identified by EDS. The thermal expansion mismatch caused by these boundary phases also weakened the interface.



Fig. 8. TEM micrographs of interphases in Al_2O_3 -sintered β -SiC and its composite, (a) amorphous silica phase and (b) crystalline aluminum silicate phase.

The stronger rising $T(c)$ curve for β -SiC/TiB₂, as compared with α -SiC/TiB₂, originated from the weak interface in the matrix and at SiC-TiB₂ interfaces. The behavior of the weak interfaces was shown in the strength degradation caused by adding TiB₂ to the SiC matrix (Fig. 4). The weak interface caused interfacial debonding, grain sliding, and grain pullout [Fig. 2(b)]. The sliding and pullout were the energy dissipating mechanisms and enhanced toughening. On the other hand, grain sliding and pullout were not easy for α -SiC/TiB₂, which gave less toughening. It has been shown that the crack resistance increases with crack extension and depends upon both the size and fraction of TiB₂ in α -SiC.¹⁰ The size and fraction of TiB₂ in β -SiC were also important. The higher volume fraction of TiB₂ in β -SiC/TiB₂ provided a chance for toughening mechanisms to operate. The larger size of TiB₂ particulates in β -SiC/TiB₂ increased the crack closure forces²⁰⁻²³ by TiB₂ bridging, sliding, and pullout, and thereby

contributed to toughened β -SiC/TiB₂ with a sharp rising T curve.

5 Conclusions

In this study, we have shown that microstructure is crucial in controlling composite performance, by comparing two kinds of SiC and SiC/TiB₂ with indentation-strength tests and microstructural evaluations. T curves of these materials were analytically deconvoluted from the indentation-strength data. TiB₂ (15 vol%) in the boron- and carbon-doped α -SiC only increased the retained strength without a significant improvement in the toughening. On the other hand, TiB₂ (30 vol%) along with the effect of Al_2O_3 sintering aid for the β -SiC/TiB₂ composite greatly improved properties with a higher retained strength in long-crack regions, better flaw-tolerance behavior and a sharply rising T curve. The different toughening behaviors for α - and β -SiC/TiB₂ were related to the weak nature of the SiC-SiC and SiC-TiB₂ interfaces as well as the fraction and size of TiB₂.

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